CS 422/522 Design & Implementation of Operating Systems

# Lecture 22: Real-Time Systems

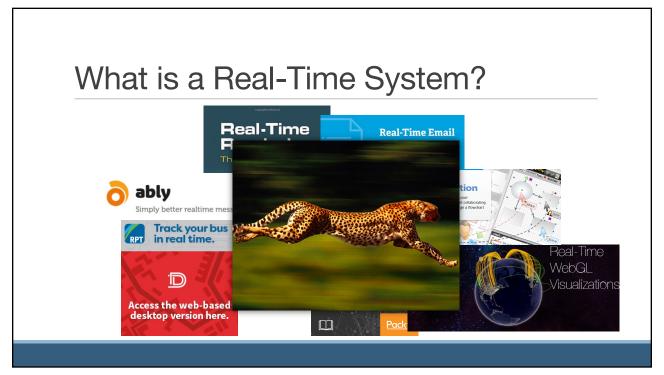
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Part of the slides are based on UIUC CS 431 Lecture Notes

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# What is a Real-Time System?









# What is a Real-Time System?

Guaranteed delivery date: Oct. 22, 2019 If you order in the next 1 hour and 13 minutes ( Details ) Items shipped from Amazon.com



Powerbeats Pro - Totally Wireless Earphones - Navy \$199.95 Prime FREE Delivery

Qty: 1 🗸

Sold by: Amazon.com Services, Inc In Stock.

Add a gift receipt
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Choose your Prime delivery option:

Tomorrow

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FREE Amazon Day Delivery

We'll deliver your orders together Choose your Amazon Day

Monday, Oct. 28 - Tuesday, Oct. 29

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Get a \$1 reward for select digital items. Details

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# Example of Real-Time Systems

Avionics and automotive systems

Radar systems

Factory process control

Robotics

Multi-media systems

. . .









### Real-Time Systems vs General-Purpose Systems









**General-Purpose Systems** 

Meeting timing requirements (analyzing the worst-case temporal behavior)

Optimizing average performance



Correctness depends on both functional and temporal aspects

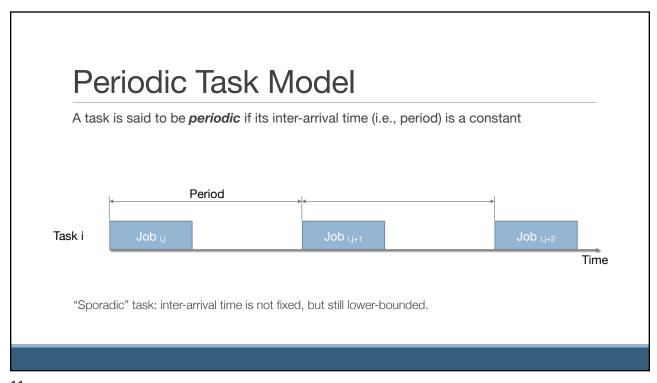
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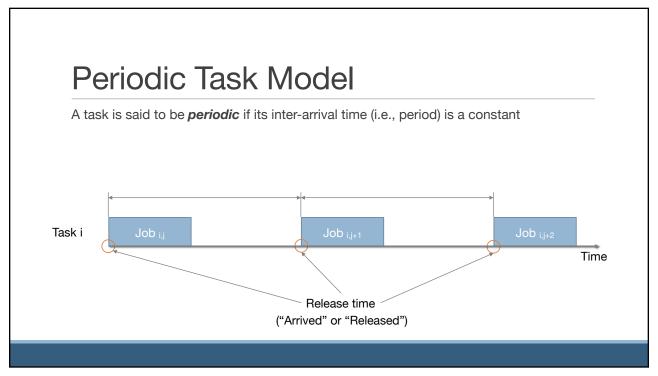
## Tasks and Jobs

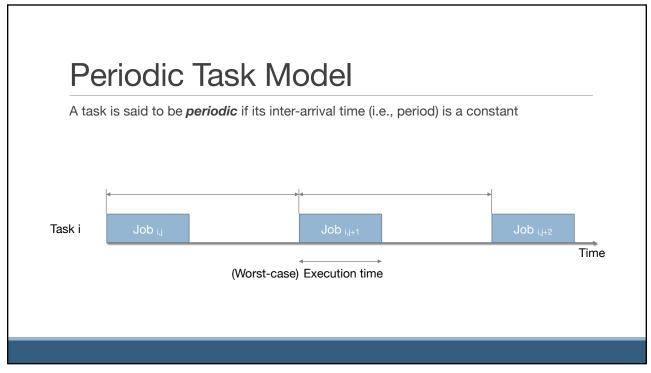
- •Task: A sequence of the same type of jobs (e.g., process or thread)
- ·Job: A unit of computation, e.g.,
  - Reading sensor values
  - Computing control commands
- Sometimes task and job are used interchangeably

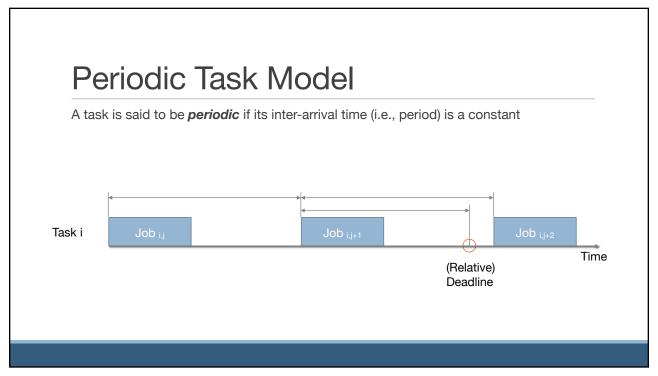
Task 1 Job <sub>1,1</sub> Job <sub>1,2</sub>

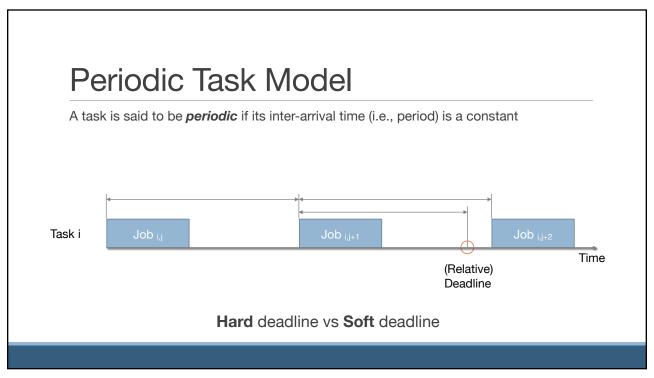
Task 2 Job <sub>2,1</sub> Job <sub>2,2</sub>

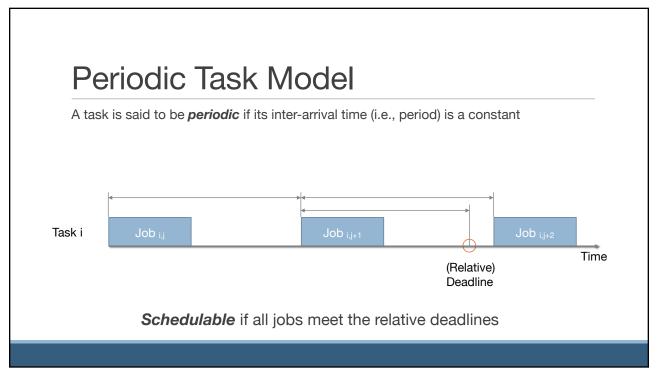












## Periodic Task Model

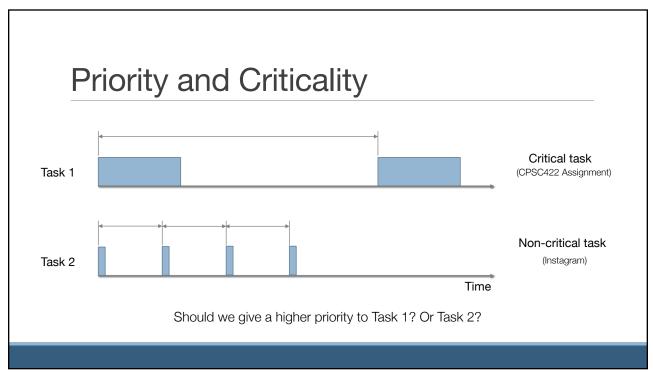
Sec.	Function	CPU	Period	Deadline	Importance
N.	avigation				
3.1		8 ms	55 ms		critical
3.2	Steering	6	80		critical
	•				
	adar Control				
3.3	Radar search or	2 2 2	80		critical
	Radar tracking	2	40		critical
	Initiate tracking	2		200	essential
Тя	rgeting				
3.4	Designate target	1		40	critical
	Confirm designation	i		200	critical
3.5	Target tracking	4	40		critical
	Target sweetening	2		40	critical
	eapon control				
3.6	Input for weapon selection	1		200	essential
3.0	Weapon selection processing	2		400	essential
	AUTO/CCIP toggle	1		200	critical
3.7	Weapon trajectory	7	100	200	critical
3.7	Reinitiate trajectory	6	100	400	essential
3.8	Weapon release	1	10	400 5 <sup>4</sup>	critical
3.6	weapon release		10	3	Citical
Co	ontrols and Displays				
3.9	HUD display	6	52		essential
	(assuming AUTO-delivery)				
	MPD HUD display	6	52		essential
3.11		8	52		essential
l	MPD button response	1		200	background
	Change display mode			200	background

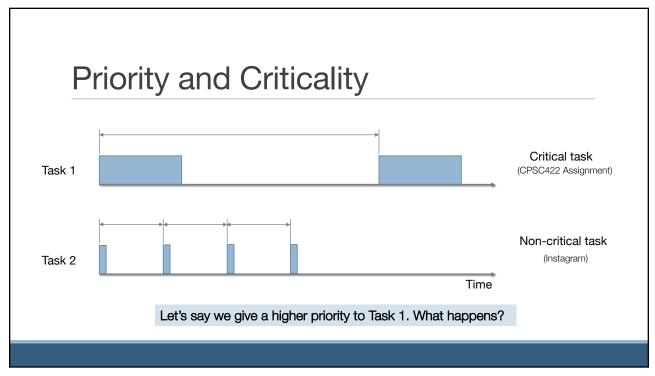
Source: Generic Avionics Software Specification

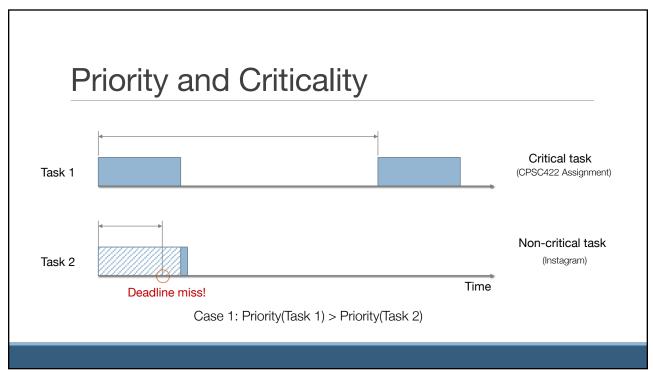
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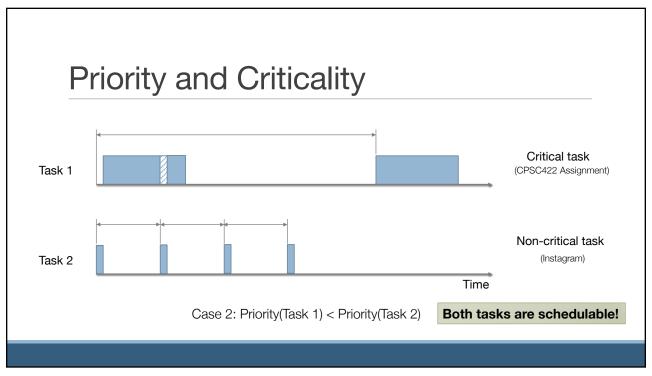
# **Priority and Criticality**

- •Priority: the order we execute ready jobs
  - Fixed-priority vs Dynamic-priority
- •Criticality: the *penalty* if a task misses its deadline
  - Usually qualitative
- •How do we assign priorities to tasks or jobs?





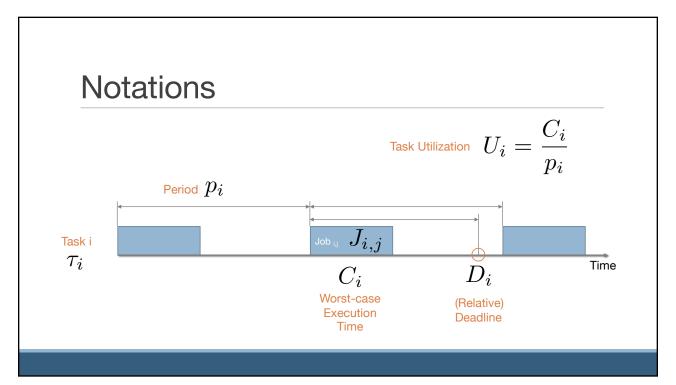




# **Priority and Criticality**

- •Importance (i.e., criticality) *may or may not* correspond to scheduling priority.
  - Priority is derived from timing requirements
- •Importance matters only when tasks can be scheduled without missing deadlines.

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# Real-Time Scheduling Algorithms

- Rate-Monotonic (RM)
  - · Assign higher priority to tasks that have higher-rate (=shorter period)
  - · Optimal fixed-priority scheduling
- Earliest Deadline First (EDF)
  - Assign higher priority to jobs that have earlier relative deadline
  - · Optimal dynamic-priority scheduling

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# Real-Time Scheduling Algorithms

#### Rate-Monotonic (RM)

- · Assign higher priority to tasks that hay
- Optimal fixed-priority scheduling

What does it mean by 'optimal' scheduling?

#### Earliest Deadline First (EDF)

- Assign higher priority to jobs that have
- Optimal dynamic-priority scheduling

# Real-Time Scheduling Algorithms

#### Rate-Monotonic (RM)

- · Assign higher priority to tasks that hay
- Optimal fixed-priority scheduling

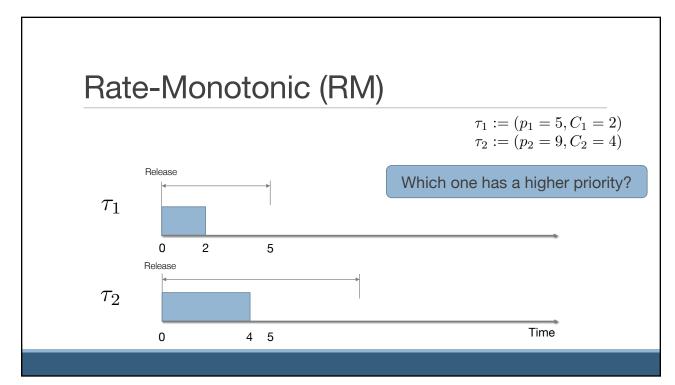
### Earliest Deadline First (EDF)

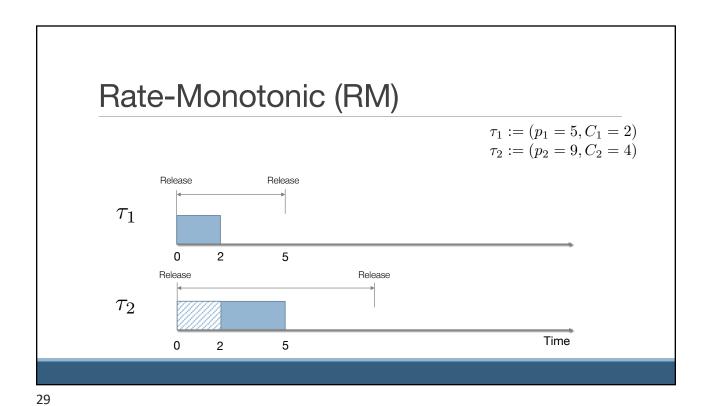
- Assign higher priority to jobs that have
- Optimal dynamic-priority scheduling

What does it mean by 'optimal' scheduling?

If a task set is not schedulable by the optimal scheduling algorithm, no other scheduling algorithms can schedule the task set

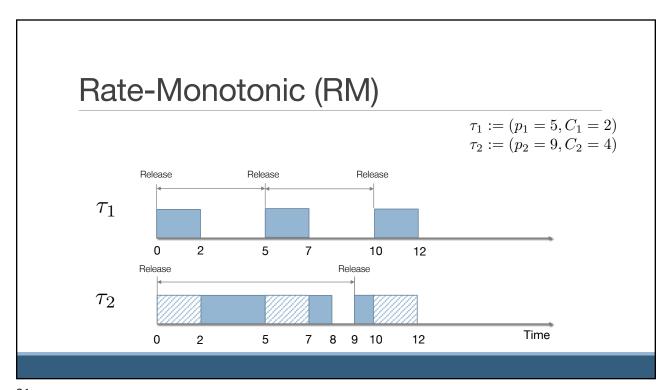
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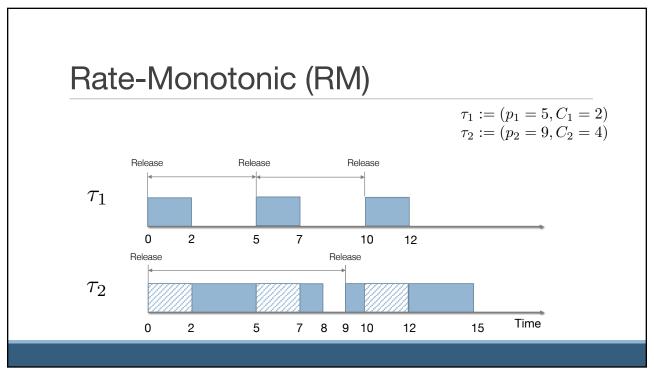


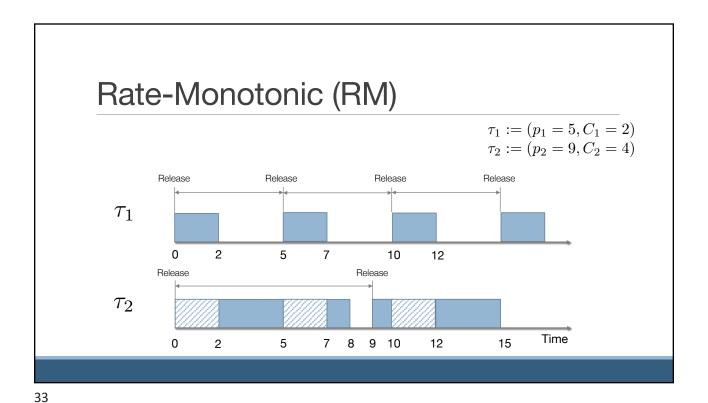


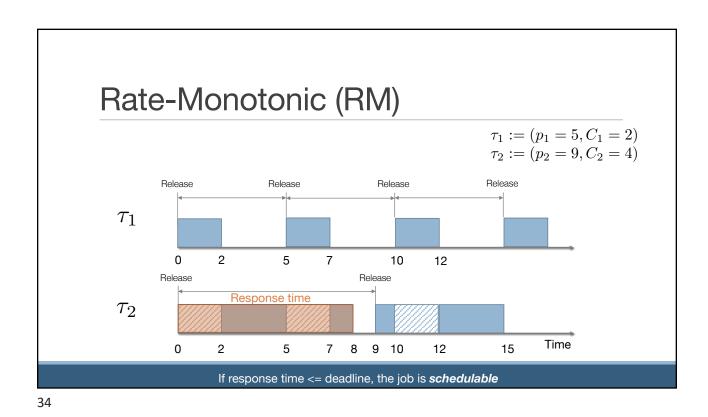
Rate-Monotonic (RM)  $\tau_1 := (p_1 = 5, C_1 = 2) \\ \tau_2 := (p_2 = 9, C_2 = 4)$ 

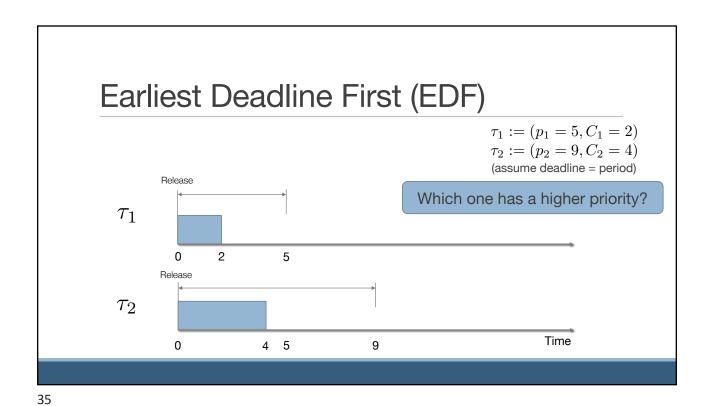
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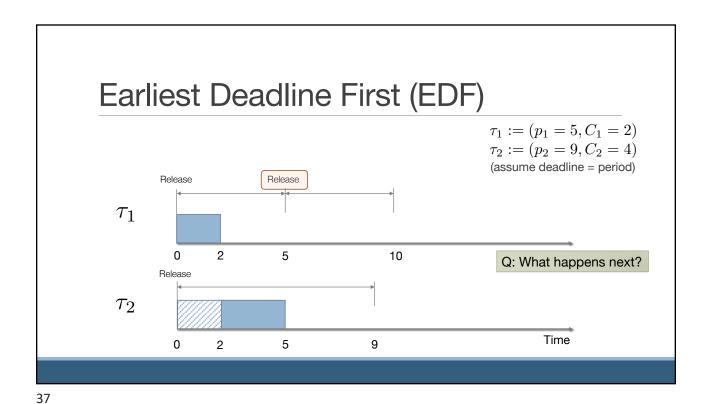






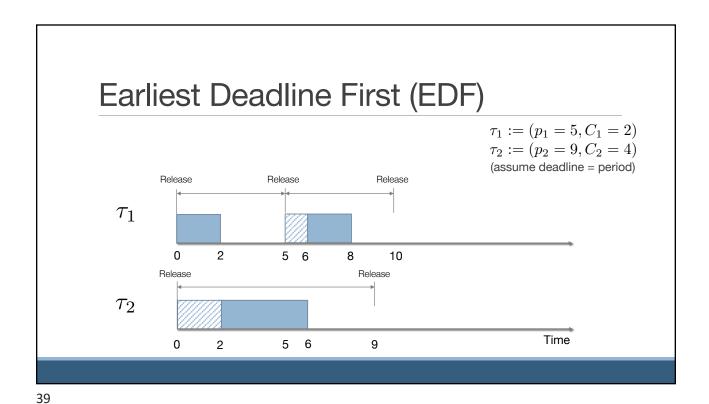


Earliest Deadline First (EDF)  $\tau_1 := (p_1 = 5, C_1 = 2) \\
\tau_2 := (p_2 = 9, C_2 = 4) \\
\text{(assume deadline = period)}$   $\tau_1 = (p_1 = 5, C_1 = 2) \\
\tau_2 := (p_2 = 9, C_2 = 4) \\
\text{(assume deadline = period)}$ 



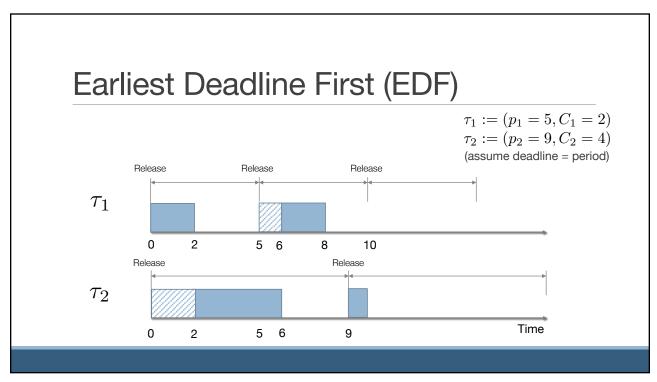
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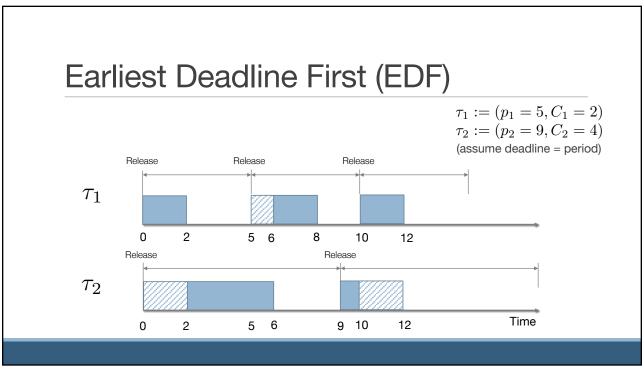
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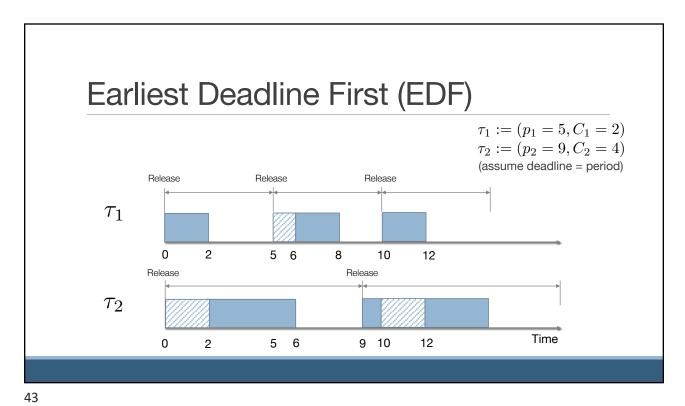


Earliest Deadline First (EDF)  $\tau_1 := (p_1 = 5, C_1 = 2)$  $\tau_2 := (p_2 = 9, C_2 = 4)$ (assume deadline = period) Release Release Release  $au_1$ 0 5 6 10 Release Release  $au_2$ Time 0 2 5 6 9

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# Schedulability Analysis

•How can we know if a set of periodic tasks is schedulable?

# Schedulability Analysis

- •How can we know if a set of periodic tasks is schedulable?
  - Exact test
  - · Utilization bound test

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## **Exact Test**

- •A.k.a. Response time analysis
- ·For fixed-priority scheduling algorithms
- •A task is said to be schedulable if and only if its **worst-case response time** is not greater than its deadline



•When is the worst-case?

### **Exact Test**

- A.k.a. Response time analysis
- ·For fixed-priority scheduling algorithms
- •A task is said to be schedulable if and only if its **worst-case response time** is not greater than its deadline



- •When is the worst-case?
  - When all higher-priority tasks are released at the same time ('Critical instant theorem' [Liu73])

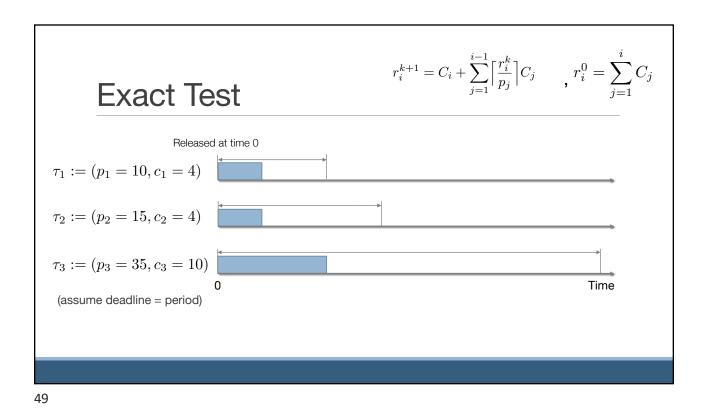
[Liu73] C. L. Liu and J. W. Layland. Scheduling algorithms for multiprogramming in a hard real-time environment. Journal of the ACM, 20(1):46-61, 1973.

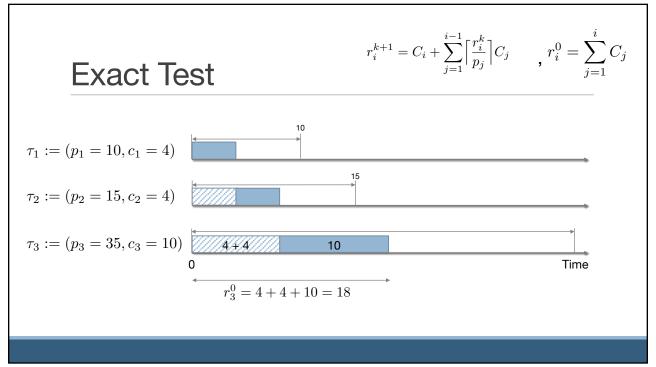
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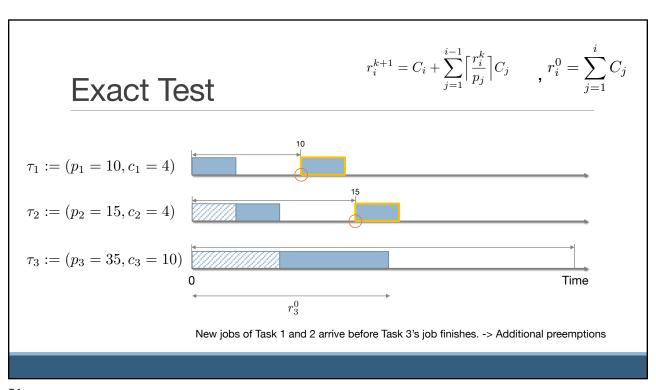
### **Exact Test**

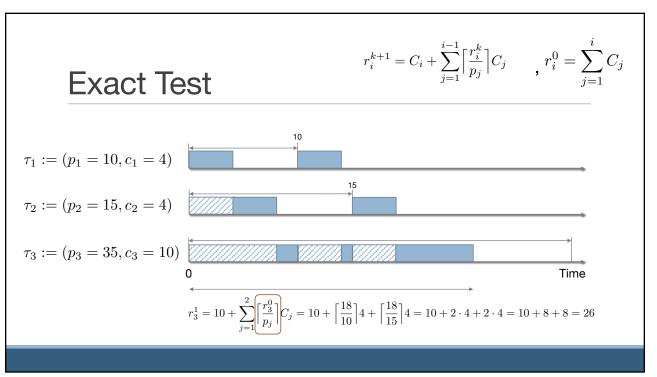
$$r_i^{k+1} = C_i + \sum_{j=1}^{i-1} \Bigl\lceil rac{r_i^k}{p_j} \Bigr
ceil C_j$$
 where  $r_i^0 = \sum_{j=1}^i C_j$ 

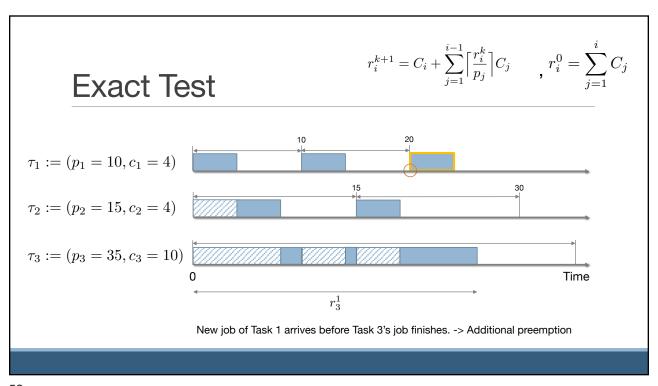
- · Iterative method
- Tasks are ordered according to their priority;  $au_1$  has the highest priority
- If  $r_i^{k+1} > D_i$  -> Unschedulable
- If  $r_i^{k+1} = r_i^k \leq D_i$  for some k -> **Schedulable**
- · Test task-by-task. If any task fails the exact test, the task set is unschedulable

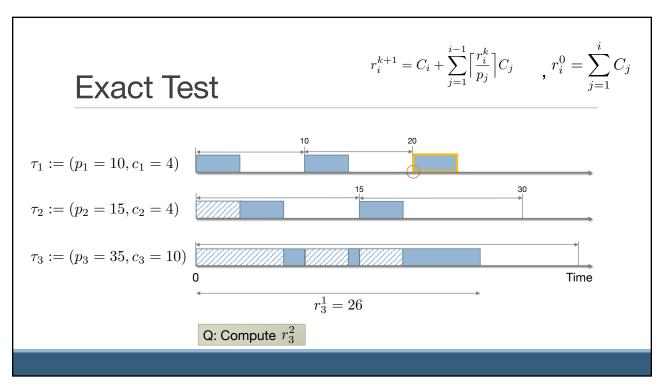


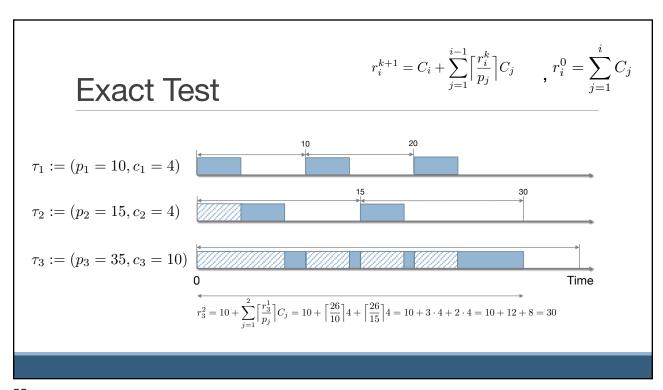


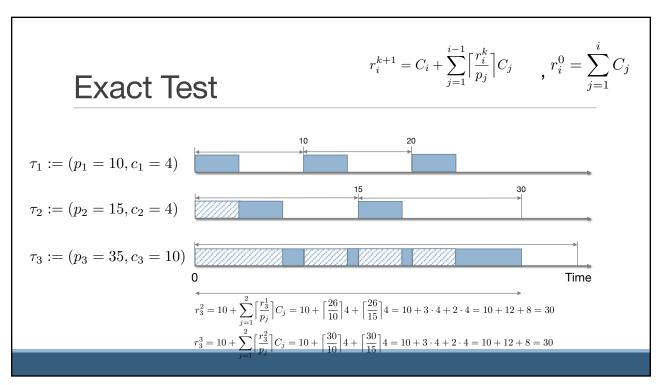






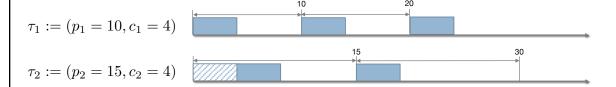








$$r_i^{k+1} = C_i + \sum_{j=1}^{i-1} ig\lceil rac{r_i^k}{p_j} ig
ceil C_j$$
 ,  $r_i^0 = \sum_{j=1}^i C_j$ 



$$\tau_3 := (p_3 = 35, c_3 = 10)$$

$$0$$

$$r_3^2 = 10 + \sum_{j=1}^2 \left\lceil \frac{r_3^1}{p_j} \right\rceil C_j = 10 + \left\lceil \frac{26}{10} \right\rceil 4 + \left\lceil \frac{26}{15} \right\rceil 4 = 10 + 3 \cdot 4 + 2 \cdot 4 = 10 + 12 + 8 = 30$$

$$r_3^3 = 10 + \sum_{j=1}^2 \left\lceil \frac{r_3^2}{p_j} \right\rceil C_j = 10 + \left\lceil \frac{30}{10} \right\rceil 4 + \left\lceil \frac{30}{15} \right\rceil 4 = 10 + 3 \cdot 4 + 2 \cdot 4 = 10 + 12 + 8 = 30$$

Worst-case Response Time (=30) < Deadline (=35)

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### **Utilization Bound Test**

**Task Utilization** 

$$U_i = \frac{C_i}{p_i}$$

Processor Utilization (n=number of tasks)

$$U = \sum_{i=1}^{n} U_i = \sum_{i=1}^{n} \frac{C_i}{p_i}$$

Utilization Bound ( $U_b$ )

Any task  $\ au_i \in \{ au_1, au_2, \dots, au_n\}$  is guaranteed to be schedulable if  $U \leq U_b$ 

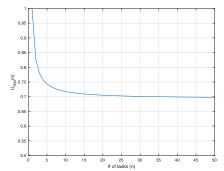
 $U_b$  depends on the scheduling algorithm, # of tasks, availability on timing information, ...

A set of *n* tasks is schedulable under RM scheduling if (see [Liu73] for proof)

$$U \le U_{RM}(n) = n(2^{1/n} - 1)$$

Example

	Ci (Execution Time)	pi (Period)	U։ (Utilization)
Task 1	20	100	?
Task 2	40	150	?
Task 3	100	350	?



[Liu73] C. L. Liu and J. W. Layland. Scheduling algorithms for multiprogramming in a hard real-time environment. Journal of the ACM, 20(1):46–61, 1973.

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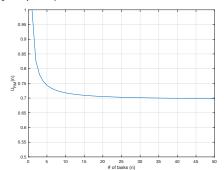
## **RM Utilization Bound**

A set of *n* tasks is schedulable under RM scheduling if (see [Liu73] for proof)

$$U \le U_{RM}(n) = n(2^{1/n} - 1)$$

Example

	C: (Execution Time)	pi (Period)	Ս։ (Utilization)
Task 1	20	100	0.200
Task 2	40	150	0.267
Task 3	100	350	0.286



1) Check the schedulability of {task 1}:

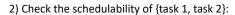
$$U_1 = 0.2 < U_{RM}(1) = 1$$

A set of *n* tasks is schedulable under RM scheduling if (see [Liu73] for proof)

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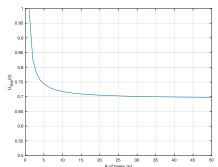
Example

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$$U_1 + U_2 \approx$$

$$U_{RM}(\ )=$$



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## **RM Utilization Bound**

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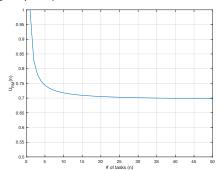
$$U \le U_{RM}(n) = n(2^{1/n} - 1)$$

Example

	Ci (Execution Time)	pi (Period)	Ս։ (Utilization)
Task 1	20	100	0.200
Task 2	40	150	0.267
Task 3	100	350	0.286



$$U_1 + U_2 \approx 0.467 < U_{RM}(2) = 0.828$$



A set of *n* tasks is schedulable under RM scheduling if (see [Liu73] for proof)

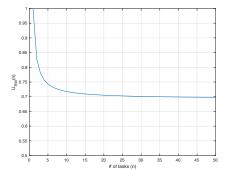
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Example

	Ci (Execution Time)	pi (Period)	U։ (Utilization)
Task 1	20	100	0.200
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$$U_1 + U_2 + U_3 \approx 0.753 < U_{RM}(3) = 0.780$$



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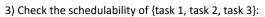
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A set of *n* tasks is schedulable under RM scheduling if (see [Liu73] for proof)

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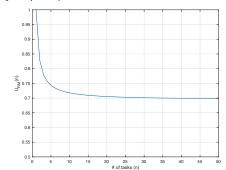
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	Ci (Execution Time)	pi (Period)	U։ (Utilization)
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$$U_1 + U_2 + U_3 \approx 0.753 < U_{RM}(3) = 0.780$$

Q: What if  $C_1=40$ ?

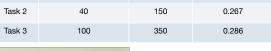


A set of n tasks is schedulable under RM scheduling if (see [Liu73] for proof)

$$U \le U_{RM}(n) = n(2^{1/n} - 1)$$

Example

	Ci (Execution Time)	pi (Period)	Ս։ (Utilization)
Task 1	40	100	0.400
Task 2	40	150	0.267
Task 3	100	350	0.286



$$U_1 + U_2 + U_3 \approx 0.953 > U_{RM}(3) = 0.780$$

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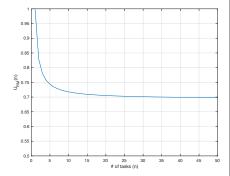
# RM Utilization Bound

A set of *n* tasks is schedulable under RM scheduling if (see [Liu73] for proof)

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Example

	Ci (Execution Time)	pi (Period)	Ui (Utilization)
Task 1	40	100	0.400
Task 2	40	150	0.267
Task 3	100	350	0.286



Q: What if  $C_1=40$ ?

 $U_1 + U_2 + U_3 \approx 0.953 > U_{RM}(3) = 0.780$ 

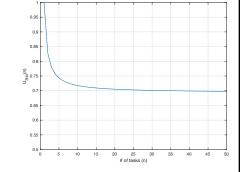
Q: Are the tasks unschedulable?

A set of *n* tasks is schedulable under RM scheduling if (see [Liu73] for proof)

$$U \le U_{RM}(n) = n(2^{1/n} - 1)$$

Example

	Ci (Execution Time)	pi (Period)	U։ (Utilization)
Task 1	40	100	0.400
Task 2	40	150	0.267
Task 3	100	350	0.286



Q: What if  $C_1=40$ ?

$$U_1 + U_2 + U_3 \approx 0.953 > U_{RM}(3) = 0.780$$

Q: Are the tasks unschedulable? A: Not necessarily. Need to do the exact test!

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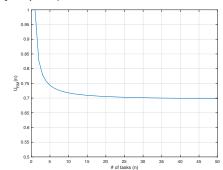
### **RM Utilization Bound**

A set of *n* tasks is schedulable under RM scheduling if (see [Liu73] for proof)

$$U \le U_{RM}(n) = n(2^{1/n} - 1)$$

Example

	C: (Execution Time)	pi (Period)	Ս։ (Utilization)
Task 1	40	100	0.400
Task 2	40	150	0.267
Task 3	100	350	0.286



Q: What is the worst-case response time of Task 3?

$$r_i^{k+1} = C_i + \sum_{j=1}^{i-1} \left\lceil \frac{r_i^k}{p_j} \right\rceil C_j$$
 ,  $r_i^0 = \sum_{j=1}^i C_j$ 

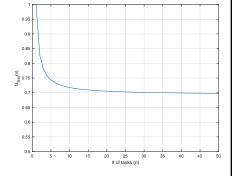
#### Utilization bound test is a sufficient condition

- of If  $U \leq U_{RM}(n)$ , the task set is guaranteed to be schedulable by RM.
- $^{\circ}~U>U_{RM}(n)$  does not necessarily mean the task set is unschedulable
  - Need to perform an exact test

### UB for any n

$$U_{RM} = \lim_{n \to \infty} U_{RM}(n) = \ln 2 \approx 0.693$$

Q: What does this mean?



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## **RM Utilization Bound**

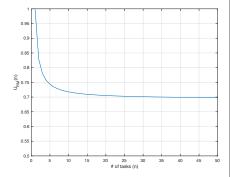
#### Utilization bound test is a sufficient condition

- $\circ$  If  $U \leq U_{RM}(n)$ , the task set is guaranteed to be schedulable by RM.
- $^{\circ}~U>U_{RM}(n)$  does not necessarily mean the task set is unschedulable
  - Need to perform an exact test

### UB for any $\boldsymbol{n}$

$$U_{RM} = \lim_{n \to \infty} U_{RM}(n) = \ln 2 \approx 0.693$$

 $_{\circ}$  That is, any task set is schedulable if  $~U \leq U_{RM}$ 



# **EDF Utilization Bound**

A set of tasks is schedulable under EDF scheduling if and only if

$$U \leq U_{EDF} = 1$$

- Sufficient and necessary condition
- Does not depend on # of tasks

	C <sub>i</sub> (Execution Time)	pi (Period)	U։ (Utilization)
Task 1	40	100	0.400
Task 2	40	150	0.267
Task 3	100	350	0.286

$$U_1 + U_2 + U_3 \approx 0.953 < U_{EDF}$$

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# RM vs EDF

EDF's utilization bound is 1 while RM's is less than 1

RM may not fully utilize the CPU

Why do we need RM?

### RM vs EDF

EDF's utilization bound is 1 while RM's is less than 1

RM may not fully utilize the CPU

### Why do we need RM?

- Simpler implementation
  - Priorities do not change
  - Some tasks may not have deadlines
- EDF is unpredictable
  - Domino effect during overloaded situation
  - A low critical task which overruns but has an earlier deadline can delay a high critical task.
  - FAA (Federal Aviation Administration) and EASA (European Aviation Safety Agency) forbid the use of EDF
  - However, EDF is desirable for budget-enforcing real-time scheduler

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## **Priority Inversion**

So far, tasks are assumed to be independent

What if tasks share data?

Synchronization!

semaphore->P();

// critical section goes here semaphore->V();

But it can be a source of priority inversion

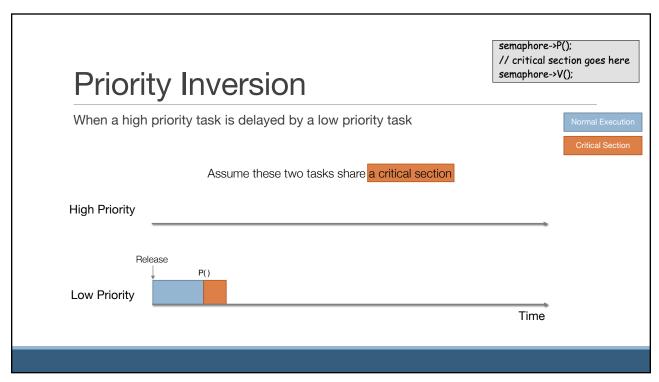
A few definitions

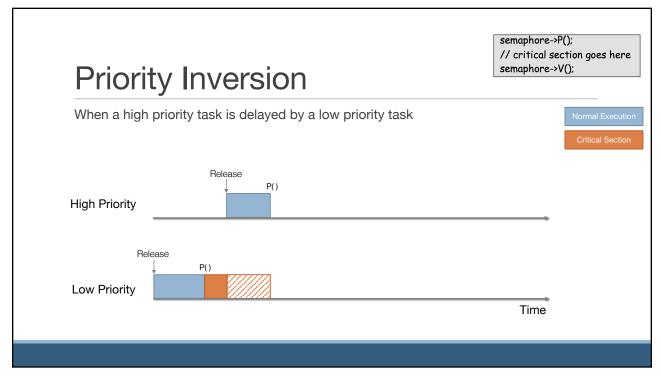
- Sychronization:
   uring atomic apprecians to
- using stemic operations to ensure cooperation between threads
   Murtual exclusion:
   ensuring that party one thread does a particular thing at a time. One
  thread doing it couldes the other, and vice versu.
   Critical section:
   Lock prevents commone from doing committing
   lock before exerting critical section; before accessing shored data
   unick who leaving, ofter done accessing shored data
   unick who leaving, ofter done accessing shored data
   unick who leaving.

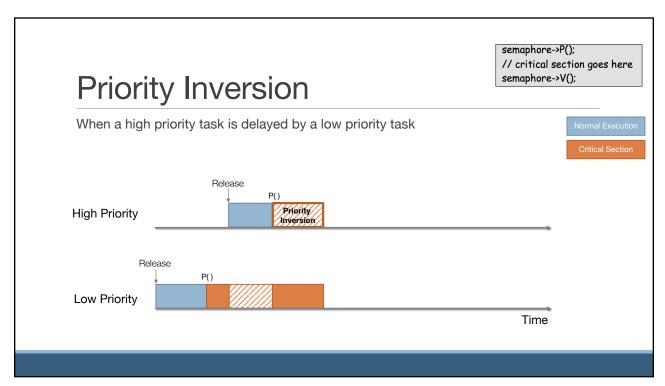
How to use semaphores

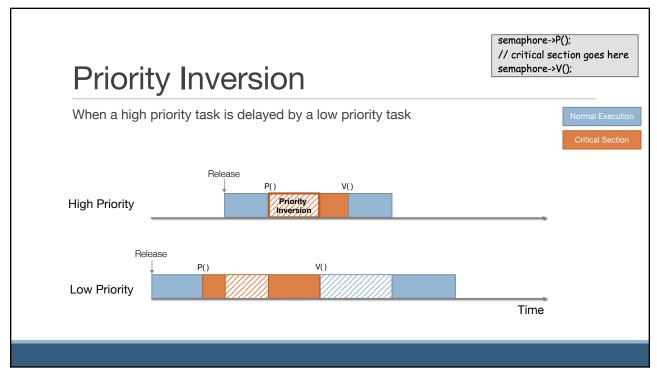
- Binary semaphores can be used for mutual exclusion:
   initial value of 1: P() is called before the critical section; and V() is called offer the critical section.
   semaphore->P():
   // critical section goes here semaphore->V():

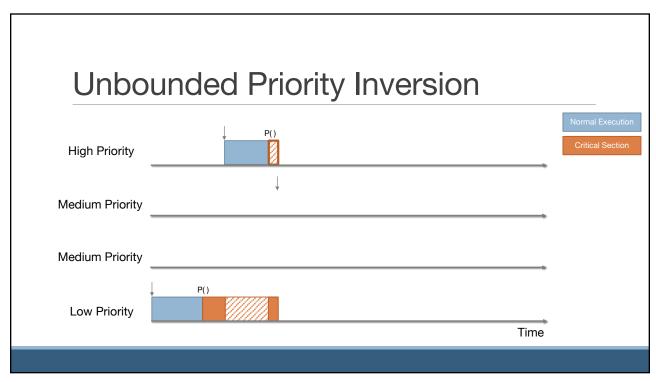
Looks familiar? Lectures 6-9

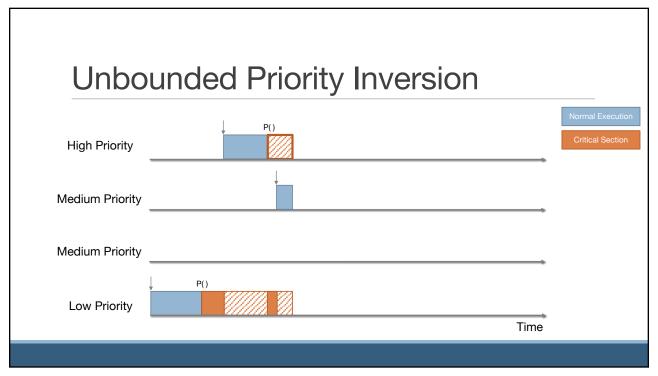


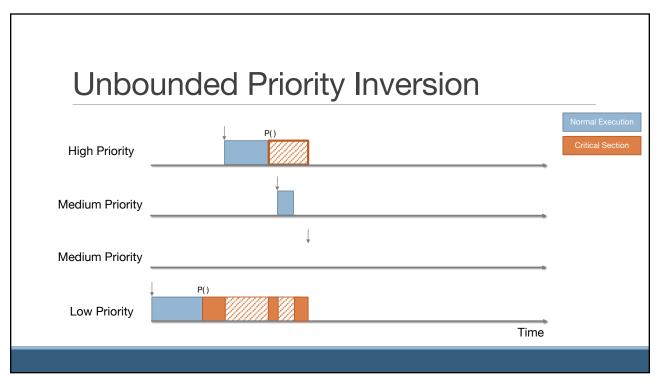


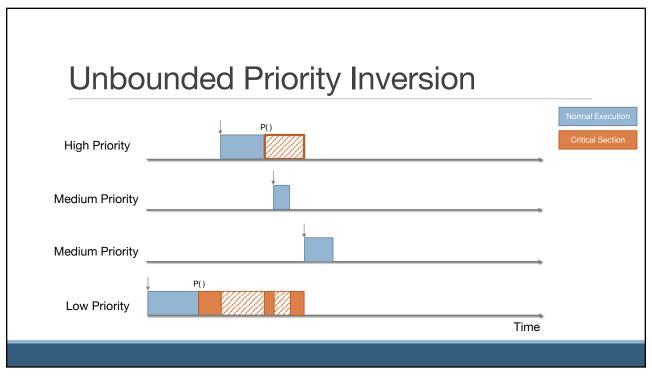


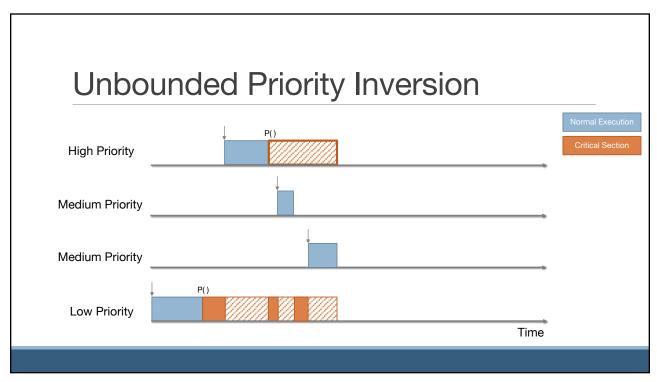


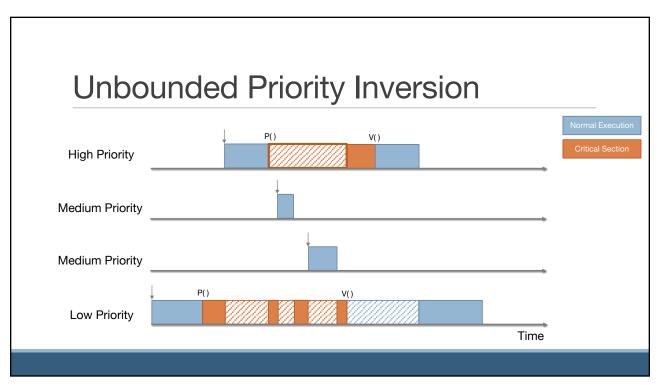


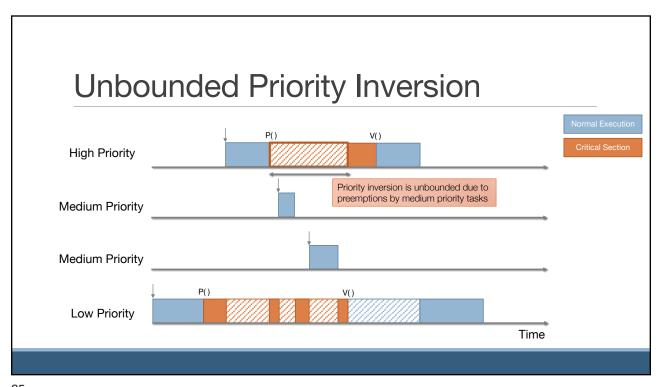


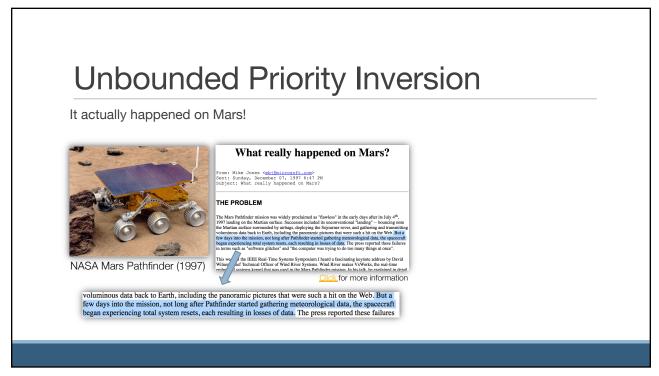


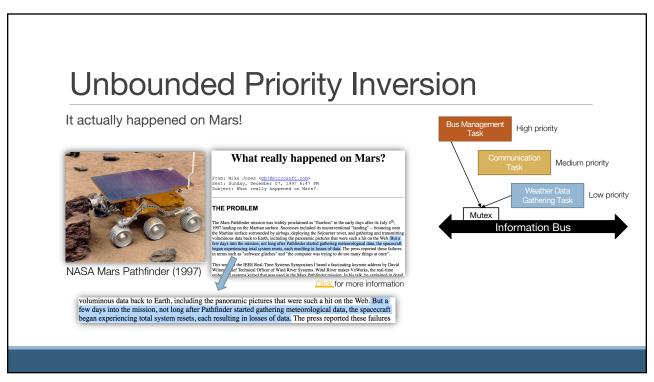


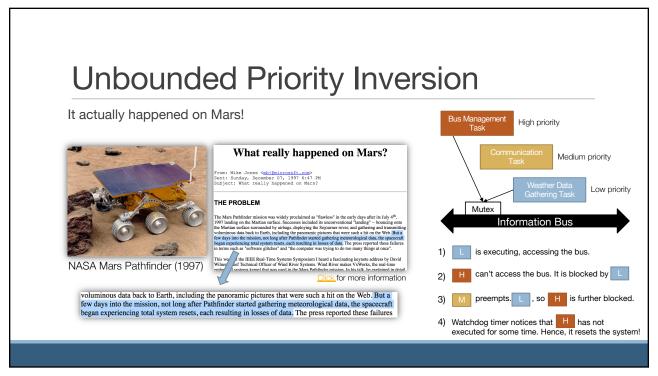


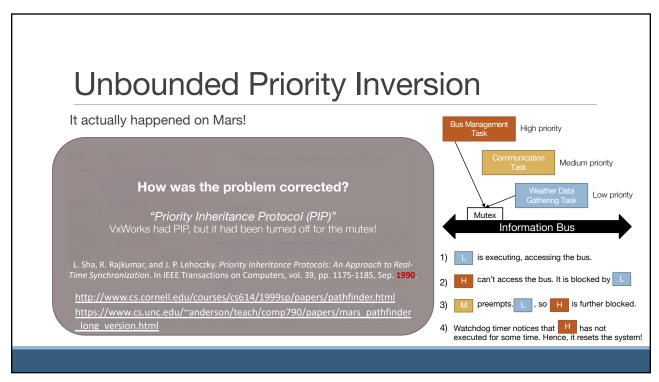


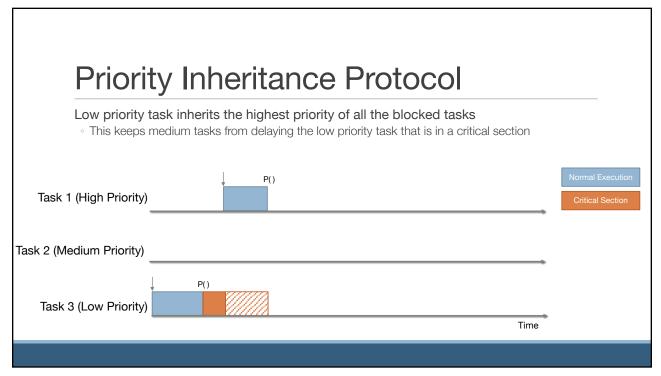


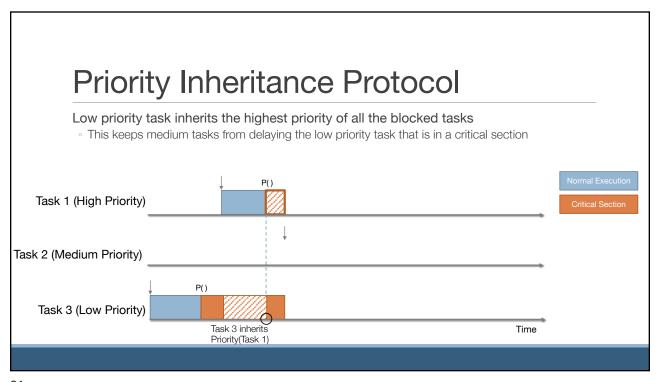


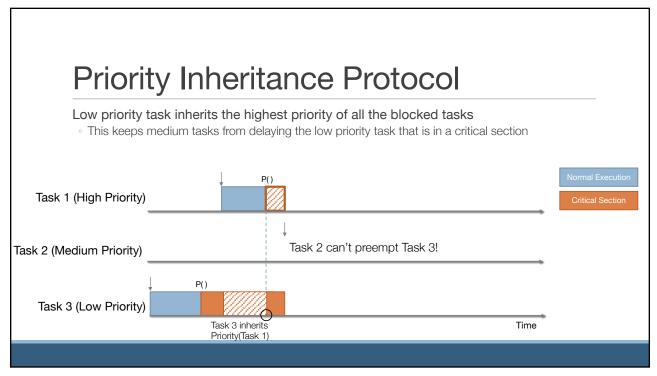


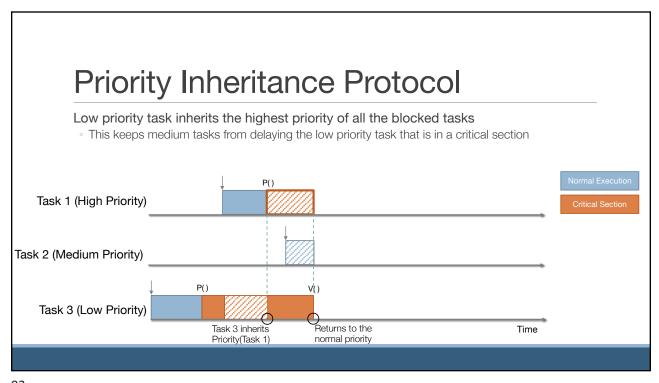


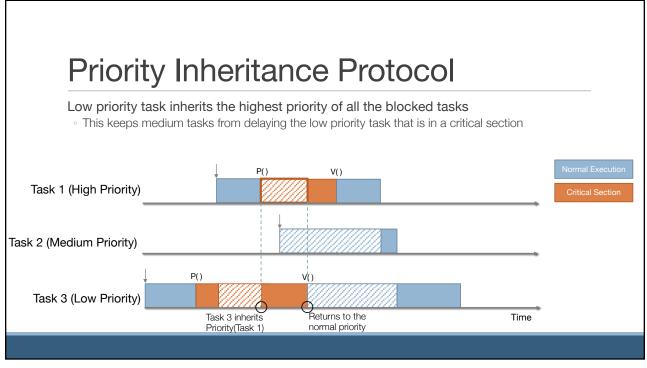












# Priority Inheritance Protocol

A job J can be blocked for at most min(n,m) times where

- $\circ$  **n** = number of lower priority jobs that could block **J**
- $\circ$  **m** = number of distinct semaphores that can be used to block **J**

But chained blocking and deadlock can happen under PIP

Solution: Priority Ceiling Protocol (PCP)

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### Priority Inheritance Protocol



https://www.youtube.com/watch?feature=oembed&v=Y6v98S1BHek

### **Priority Ceiling Protocol**

#### Priority ceiling of a semaphore

• The priority of the highest priority task that may use the semaphore

#### **Key Idea**

- A job J is allowed to enter a critical section only if its priority is higher than all priority ceilings of the semaphores currently locked by jobs other than J
  - Thus, it can never be blocked by lower priority jobs until its completion!
- When a job gets a semaphore, PCP guarantees that this job will get all the semaphores that it ever needs.
- Hence, PCP prevents chained blocking and deadlock.

#### For more information, see

L. Sha, R. Rajkumar, and J. P. Lehoczky. *Priority Inheritance Protocols: An Approach to Real-Time Synchronization*. In IEEE Transactions on Computers, vol. 39, pp. 1175-1185, Sep. 1990.