
CS 422/522 Design & Implementation
of Operating Systems

Lecture 10: Multi-Object Synchronization

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Multi-object programs

- ◆ What happens when we try to synchronize across multiple objects in a large program?
 - Each object with its own lock, condition variables
 - Is locking modular?
- ◆ Performance
- ◆ Semantics/correctness
- ◆ Deadlock
- ◆ Eliminating locks

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Synchronization performance

- ◆ A program with lots of concurrent threads can still have poor performance on a multiprocessor:
 - Overhead of creating threads, if not needed
 - Lock contention: only one thread at a time can hold a given lock
 - Shared data protected by a lock may ping back and forth between cores
 - False sharing: communication between cores even for data that is not shared

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Topics

- ◆ Multiprocessor cache coherence
- ◆ MCS locks (if locks are mostly busy)
- ◆ RCU locks (if locks are mostly busy, and data is mostly read-only)

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Multiprocessor cache coherence

- ◆ Scenario:
 - Thread A modifies data inside a critical section & releases lock
 - Thread B acquires lock and reads data
- ◆ Easy if all accesses go to main memory
 - Thread A changes main memory; thread B reads it
- ◆ What if new data is cached at processor A?
- ◆ What if old data is cached at processor B

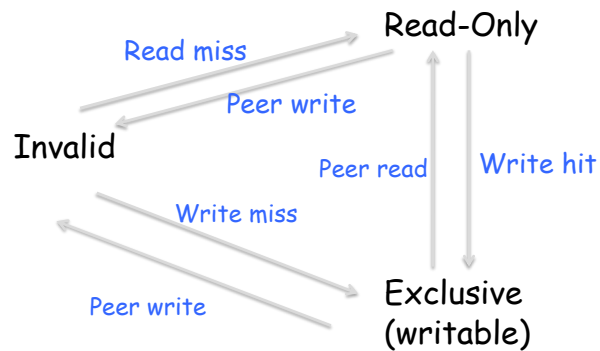
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Write-back cache coherence

- ◆ Cache coherence = system behaves as if there is one copy of the data
 - If data is only being read, any number of caches can have a copy
 - If data is being modified, at most one cached copy
- ◆ On write: (get ownership)
 - Invalidate all cached copies, before doing write
 - Modified data stays in cache ("write back")
- ◆ On read:
 - Fetch value from owner or from memory

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Cache state machine



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Directory-based cache coherence

- ◆ How do we know which cores have a location cached?
 - Hardware keeps track of all cached copies
 - On a read miss, if held exclusive, fetch latest copy and invalidate that copy
 - On a write miss, invalidate all copies
- ◆ Read-modify-write instructions
 - Fetch cache entry exclusive, prevent any other cache from reading the data until instruction completes

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A simple critical section

```
// A counter protected by a spinlock
Counter::Increment() {
    while (test_and_set(&lock))
        ;
    value++;
    lock = FREE;
    memory_barrier();
}
```

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A simple test of cache Behavior

Array of 1K counters, each protected by a separate spinlock

- Array small enough to fit in cache

- ◆ Test 1: one thread loops over array
- ◆ Test 2: two threads loop over different arrays
- ◆ Test 3: two threads loop over single array
- ◆ Test 4: two threads loop over alternate elements in single array

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Results (64 core AMD Opteron)

One thread, one array	51 cycles
Two threads, two arrays	52 cycles
Two threads, one array	197 cycles
Two threads, odd/even	127 cycles

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Reducing lock contention

- ◆ Fine-grained locking
 - Partition object into subsets, each protected by its own lock
 - Example: hash table buckets
- ◆ Per-processor data structures
 - Partition object so that most/all accesses are made by one processor
 - Example: per-processor heap
- ◆ Ownership/staged architecture
 - Only one thread at a time accesses shared data
 - Example: pipeline of threads

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What if locks are still mostly busy?

- ◆ MCS Locks
 - Optimize lock implementation for when lock is contended
- ◆ RCU (read-copy-update)
 - Efficient readers/writers lock used in Linux kernel
 - Readers proceed without first acquiring lock
 - Writer ensures that readers are done
- ◆ Both rely on atomic read-modify-write instructions

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The problem with test-and-set

```
Counter::Increment() {
    while (test_and_set(&lock))
        ;
    value++;
    lock = FREE;
    memory_barrier();
}
```

What happens if many processors try to acquire the lock at the same time?

- Hardware doesn't prioritize FREE

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The problem with test-&-test-and-set

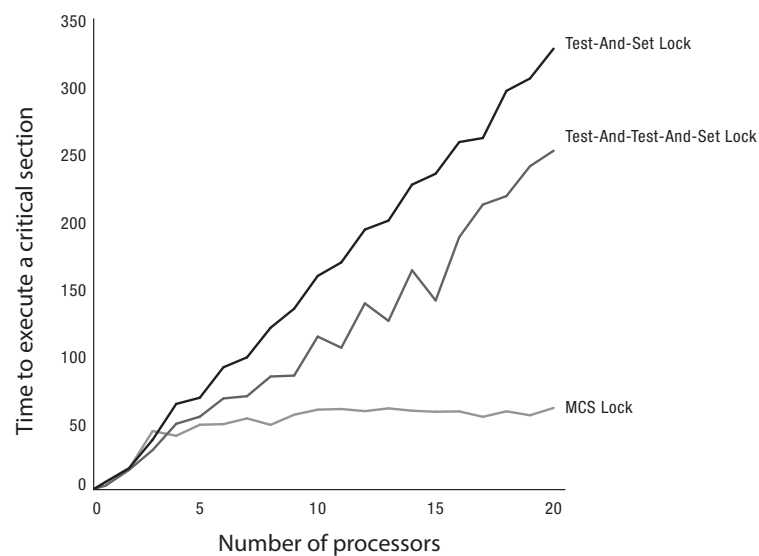
```
Counter::Increment() {
    while (lock == BUSY || test_and_set(&lock))
        ;
    value++;
    lock = FREE;
    memory_barrier();
}
```

What happens if many processors try to acquire the lock?

- Lock value pings between caches

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Test (and test) and set performance



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Some Approaches

- ◆ Insert a delay in the spin loop
 - Helps but acquire is slow when not much contention
- ◆ Spin adaptively
 - No delay if few waiting
 - Longer delay if many waiting
 - Guess number of waiters by how long you wait
- ◆ MCS
 - Create a linked list of waiters using `compareAndSwap`
 - Spin on a per-processor location

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Atomic CompareAndSwap

- ◆ Operates on a memory word
- ◆ Check that the value of the memory word hasn't changed from what you expect
 - E.g., no other thread did `compareAndSwap` first
- ◆ If it has changed, return an error (and loop)
- ◆ If it has not changed, set the memory word to a new value

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MCS Lock

- ◆ Maintain a list of threads waiting for the lock
 - Front of list holds the lock
 - MCSLock::tail is last thread in list
 - New thread uses CompareAndSwap to add to the tail
 - ◆ Lock is passed by setting next->needToWait = FALSE;
 - Next thread spins while its needToWait is TRUE
- ```
TCB {
 TCB *next; // next in line
 bool needToWait;
}
MCSLock {
 Queue *tail = NULL; // end of line
}
```

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## MCS Lock implementation

```
class MCSLock {
private: Queue *tail = NULL;
}

MCSLock::release() {
 if (compareAndSwap(&tail,
 myTCB, NULL)) {
 // if tail == myTCB, no one is waiting.
 // MCSLock is now free.
 } else {
 // someone is waiting
 while (myTCB->next == NULL)
 ; // spin until next is set
 // Tell next thread to proceed
 myTCB->next->needToWait = FALSE;
 }
}

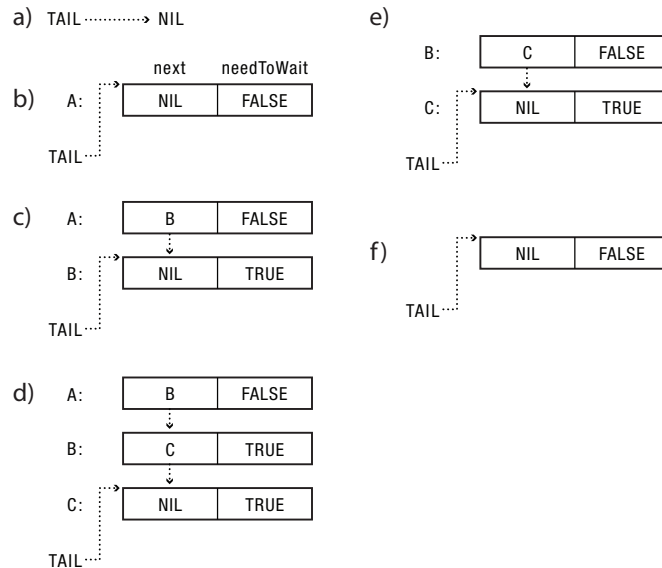
MCSLock::acquire() {
 Queue *oldTail = tail;
 myTCB->next = NULL;

 while (!compareAndSwap(&tail,
 oldTail, &myTCB)) {
 // try again if someone changed tail
 oldTail = tail;
 }

 if (oldTail != NULL) {
 // Need to wait
 myTCB->needToWait = TRUE;
 memory_barrier();
 oldTail->next = myTCB;
 while (myTCB->needToWait)
 ; // spin
 }
}
```

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## MCSLock in operation



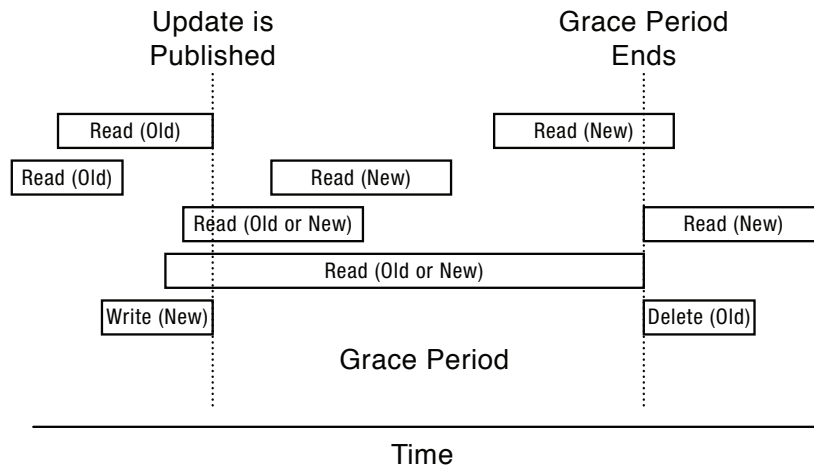
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## Read-Copy-Update

- ◆ **Goal: very fast reads to shared data**
  - Reads proceed without first acquiring a lock
  - OK if write is (very) slow
- ◆ **Restricted update**
  - Writer computes new version of data structure
  - Publishes new version with a single atomic instruction
- ◆ **Multiple concurrent versions**
  - Readers may see old or new version
- ◆ **Integration with thread scheduler**
  - Guarantee all readers complete within grace period, and then garbage collect old version

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## Read-Copy-Update



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## Read-Copy-Update implementation

- ◆ Readers disable interrupts on entry
  - Guarantees they complete critical section in a timely fashion
  - No read or write lock
- ◆ Writer
  - Acquire write lock
  - Compute new data structure
  - Publish new version with atomic instruction
  - Release write lock
  - Wait for time slice on each CPU
  - Only then, garbage collect old version of data structure

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## Non-blocking synchronization

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- ◆ Goal: data structures that can be read/modified without acquiring a lock
  - No lock contention!
  - No deadlock!
- ◆ General method using compareAndSwap
  - Create copy of data structure
  - Modify copy
  - Swap in new version iff no one else has
  - Restart if pointer has changed

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## Deadlock definition

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- ◆ Resource: any (passive) thing needed by a thread to do its job (CPU, disk space, memory, lock)
  - Preemptable: can be taken away by OS
  - Non-preemptable: must leave with thread
- ◆ Starvation: thread waits indefinitely
- ◆ Deadlock: circular waiting for resources
  - Deadlock => starvation, but not vice versa

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### Example: two locks

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Thread A

```
lock1.acquire();
lock2.acquire();
lock2.release();
lock1.release();
```

Thread B

```
lock2.acquire();
lock1.acquire();
lock1.release();
lock2.release();
```

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### Bidirectional bounded buffer

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Thread A

```
buffer1.put(data);
buffer1.put(data);
```

```
buffer2.get();
buffer2.get();
```

Thread B

```
buffer2.put(data);
buffer2.put(data);
```

```
buffer1.get();
buffer1.get();
```

Suppose buffer1 and buffer2 both start almost full.

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## Two locks and a condition variable

Thread A

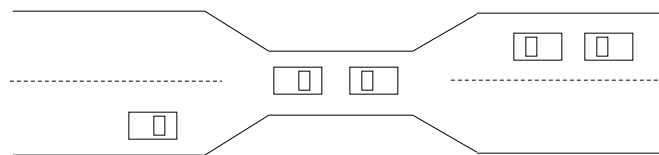
```
lock1.acquire();
...
lock2.acquire();
while (need to wait) {
 condition.wait(lock2);
}
lock2.release();
...
lock1.release();
```

Thread B

```
lock1.acquire();
...
lock2.acquire();
...
condition.signal(lock2);
...
lock2.release();
...
lock1.release();
```

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## The bridge-crossing example



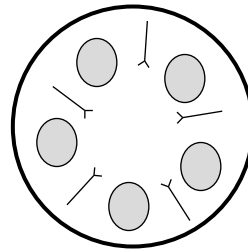
- ◆ Traffic only in one direction.
- ◆ Each section of a bridge can be viewed as a resource.
- ◆ If a deadlock occurs, it can be resolved if one car backs up (preempt resources and rollback).
- ◆ Several cars may have to be backed up if a deadlock occurs.
- ◆ Starvation is possible.

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## The dining philosophers problem

- ◆ Five philosophers around a table --- thinking or eating
- ◆ Five plates of spaghetti + five forks (placed between each plate)
- ◆ The spaghetti is so slippery that a philosopher needs two forks to eat it.

```
void philosopher (int i) {
 while (TRUE) {
 think();
 take_fork (i);
 take_fork ((i+1) % 5);
 eat();
 put_fork (i);
 put_fork ((i+1) % 5);
 }
}
```



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## Necessary conditions for deadlock

- ◆ Limited access to resources
  - If infinite resources, no deadlock!
- ◆ No preemption
  - If resources are virtual, can break deadlock
- ◆ Multiple independent requests
  - "wait while holding"
- ◆ Circular chain of requests

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## Question

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- ◆ How does Dining Philosophers meet the necessary conditions for deadlock?
  - Limited access to resources
  - No preemption
  - Multiple independent requests (wait while holding)
  - Circular chain of requests
- ◆ How can we modify Dining Philosophers to prevent deadlock?

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## Preventing deadlock

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- ◆ Exploit or limit program behavior
  - Limit program from doing anything that might lead to deadlock
- ◆ Predict the future
  - If we know what program will do, we can tell if granting a resource might lead to deadlock
- ◆ Detect and recover
  - If we can rollback a thread, we can fix a deadlock once it occurs

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## Exploit or limit behavior

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- ◆ Provide enough resources
  - How many chopsticks are enough?
- ◆ Eliminate wait while holding
  - Release lock when calling out of module
  - Telephone circuit setup
- ◆ Eliminate circular waiting
  - Lock ordering: always acquire locks in a fixed order
  - Example: move file from one directory to another

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## Example

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| Thread 1                 | Thread 2      |
|--------------------------|---------------|
| 1. Acquire A             | 1.            |
| 2.                       | 2. Acquire B  |
| 3. Acquire C             | 3.            |
| 4.                       | 4. Wait for A |
| 5. If (maybe) Wait for B |               |

How can we make sure to avoid deadlock?

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## System model

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- ◆ Resource types  $R_1, R_2, \dots, R_m$   
*CPU cycles, memory space, I/O devices*
- ◆ Each resource type  $R_i$  has  $W_i$  instances.
- ◆ Each process utilizes a resource as follows:
  - request
  - use
  - release

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## Resource-allocation graph (1)

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*A set of vertices  $V$  and a set of edges  $E$ .*

- ◆  $V$  is partitioned into two types:
  - $P = \{P_1, P_2, \dots, P_n\}$ , the set consisting of all the processes in the system.
  - $R = \{R_1, R_2, \dots, R_m\}$ , the set consisting of all resource types in the system.
- ◆ request edge - directed edge  $P_i \rightarrow R_j$
- ◆ assignment edge - directed edge  $R_j \rightarrow P_i$

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## Resource-allocation graph (2)

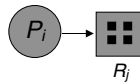
◆ Process



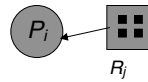
◆ Resource type with 4 instances



◆  $P_i$  requests instance of  $R_j$

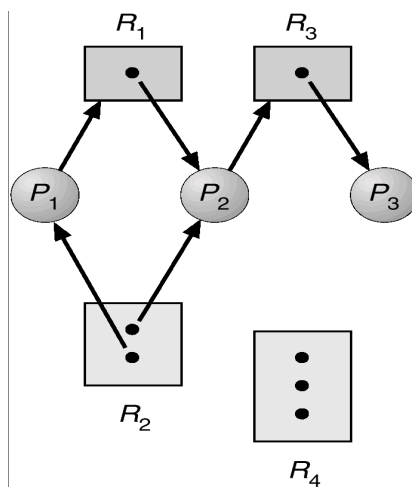


◆  $P_i$  is holding an instance of  $R_j$



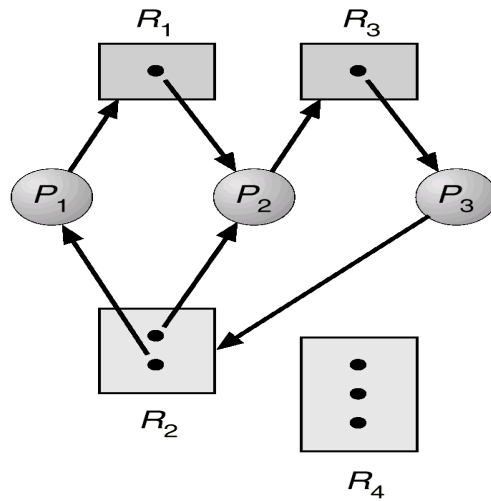
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## Example: resource-allocation graph



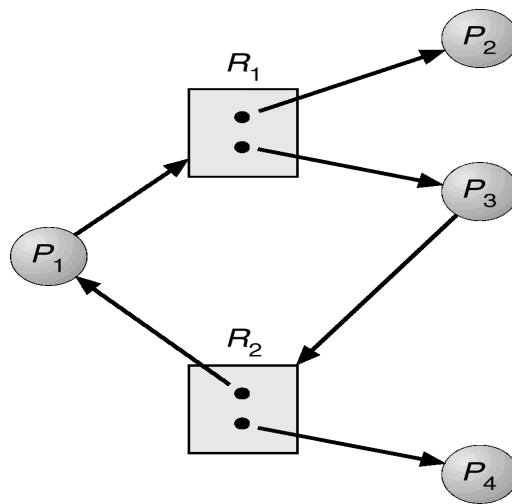
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### Resource-allocation graph with a deadlock



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### Resource-allocation graph with a cycle but no deadlock



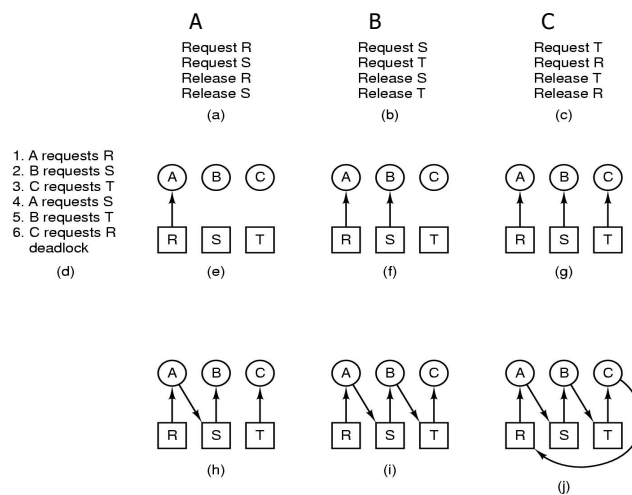
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## Resource allocation graph vs. deadlock?

- ◆ If graph contains no cycles  $\Rightarrow$  no deadlock.
- ◆ If graph contains a cycle  $\Rightarrow$ 
  - if only one instance per resource type, then deadlock.
  - if several instances per resource type, possibility of deadlock.

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## How deadlocks occur?

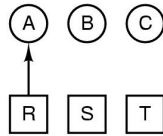


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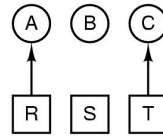
## How deadlocks can be avoided

1. A requests R
2. C requests T
3. A requests S
4. C requests R
5. A releases R
6. A releases S

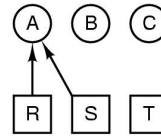
(k)



(l)

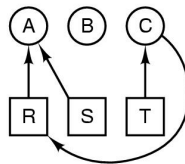


(m)

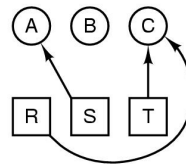


(n)

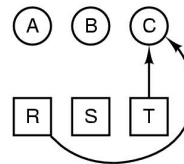
*Block  
process B  
when it asks  
for S.*



(o)



(p)



(q)

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## Deadlock detection: data structures

Resources in existence  
( $E_1, E_2, E_3, \dots, E_m$ )

Resources available  
( $A_1, A_2, A_3, \dots, A_m$ )

Current allocation matrix

$$\begin{bmatrix} C_{11} & C_{12} & C_{13} & \cdots & C_{1m} \\ C_{21} & C_{22} & C_{23} & \cdots & C_{2m} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ C_{n1} & C_{n2} & C_{n3} & \cdots & C_{nm} \end{bmatrix}$$

Row n is current allocation  
to process n

Request matrix

$$\begin{bmatrix} R_{11} & R_{12} & R_{13} & \cdots & R_{1m} \\ R_{21} & R_{22} & R_{23} & \cdots & R_{2m} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ R_{n1} & R_{n2} & R_{n3} & \cdots & R_{nm} \end{bmatrix}$$

Row 2 is what process 2 needs

Data structures needed by deadlock detection algorithm

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## Deadlock detection: example

$$E = \begin{pmatrix} 4 & 2 & 3 & 1 \end{pmatrix} \quad A = \begin{pmatrix} 2 & 1 & 0 & 0 \end{pmatrix}$$

Tape drives   Plotters   Scanners   CD Roms      Tape drives   Plotters   Scanners   CD Roms

Current allocation matrix

$$C = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 2 & 0 & 0 & 1 \\ 0 & 1 & 2 & 0 \end{bmatrix}$$

Request matrix

$$R = \begin{bmatrix} 2 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 2 & 1 & 0 & 0 \end{bmatrix}$$

An example for the deadlock detection algorithm

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## Methods for handling deadlocks

- ◆ Ensure that the system will *never* enter a deadlock state. *(deadlock prevention and avoidance)*
  - \* problems: low device utilization, reduced throughput
  - \* avoidance also requires prediction of resource needs
- ◆ Allow the system to enter a deadlock state and then recover. *(deadlock detection and recovery)*
  - \* costly; sometimes impossible to recover
- ◆ Ignore the problem and pretend that deadlocks never occur in the system; used by most operating systems, including UNIX.

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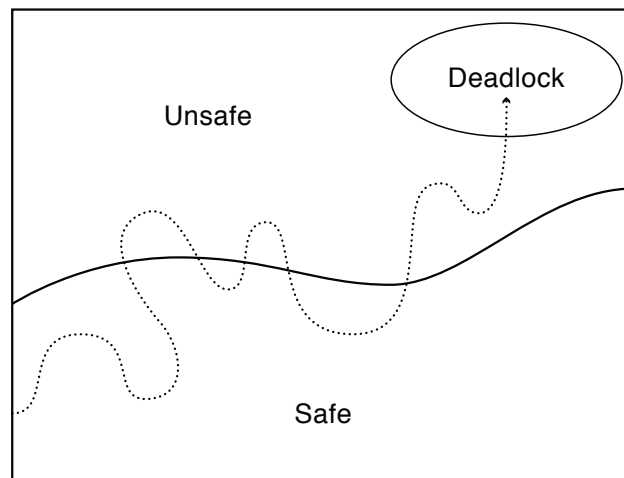


## Deadlock dynamics

- ◆ Safe state:
  - For any possible sequence of future resource requests, it is possible to eventually grant all requests
  - May require waiting even when resources are available!
- ◆ Unsafe state:
  - Some sequence of resource requests can result in deadlock
  -
- ◆ Doomed state:
  - All possible computations lead to deadlock

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## Possible system states



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## Safe and unsafe states

| Has Max |   |   | Has Max |   |   | Has Max |   |   | Has Max |   |   | Has Max |   |   |
|---------|---|---|---------|---|---|---------|---|---|---------|---|---|---------|---|---|
| A       | 3 | 9 | A       | 3 | 9 | A       | 3 | 9 | A       | 3 | 9 | A       | 3 | 9 |
| B       | 2 | 4 | B       | 4 | 4 | B       | 0 | — | B       | 0 | — | B       | 0 | — |
| C       | 2 | 7 | C       | 2 | 7 | C       | 2 | 7 | C       | 7 | 7 | C       | 0 | — |
| Free: 3 |   |   | Free: 1 |   |   | Free: 5 |   |   | Free: 0 |   |   | Free: 7 |   |   |
| (a)     |   |   | (b)     |   |   | (c)     |   |   | (d)     |   |   | (e)     |   |   |

Demonstration that the state in (a) is safe

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## Safe and unsafe states

| Has Max |   |   | Has Max |   |   | Has Max |   |   | Has Max |   |   |
|---------|---|---|---------|---|---|---------|---|---|---------|---|---|
| A       | 3 | 9 | A       | 4 | 9 | A       | 4 | 9 | A       | 4 | 9 |
| B       | 2 | 4 | B       | 2 | 4 | B       | 4 | 4 | B       | — | — |
| C       | 2 | 7 | C       | 2 | 7 | C       | 2 | 7 | C       | 2 | 7 |
| Free: 3 |   |   | Free: 2 |   |   | Free: 0 |   |   | Free: 4 |   |   |
| (a)     |   |   | (b)     |   |   | (c)     |   |   | (d)     |   |   |

Demonstration that the state in (b) is not safe

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## Predict the future

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- ◆ Banker's algorithm
  - State maximum resource needs in advance
  - Allocate resources dynamically when resource is needed -- wait if granting request would lead to deadlock
  - Request can be granted if some sequential ordering of threads is deadlock free

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## Banker's algorithm

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- ◆ Grant request iff result is a safe state
- ◆ Sum of maximum resource needs of current threads can be greater than the total resources
  - Provided there is some way for all the threads to finish without getting into deadlock
- ◆ Example: proceed iff
  - total available resources - # allocated  $\geq$  max remaining that might be needed by this thread in order to finish
  - Guarantees this thread can finish

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## Banker's algorithm for a single resource

|   | Has | Max |
|---|-----|-----|
| A | 0   | 6   |
| B | 0   | 5   |
| C | 0   | 4   |
| D | 0   | 7   |

Free: 10

(a)

|   | Has | Max |
|---|-----|-----|
| A | 1   | 6   |
| B | 1   | 5   |
| C | 2   | 4   |
| D | 4   | 7   |

Free: 2

(b)

|   | Has | Max |
|---|-----|-----|
| A | 1   | 6   |
| B | 2   | 5   |
| C | 2   | 4   |
| D | 4   | 7   |

Free: 1

(c)

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## Banker's algorithm for multiple resources

|   | Process | Tape drives | Plotters | Scanners | CD ROMs |
|---|---------|-------------|----------|----------|---------|
| A | 3       | 0           | 1        | 1        |         |
| B | 0       | 1           | 0        | 0        |         |
| C | 1       | 1           | 1        | 0        |         |
| D | 1       | 1           | 0        | 1        |         |
| E | 0       | 0           | 0        | 0        |         |

Resources assigned

|   | Process | Tape drives | Plotters | Scanners | CD ROMs |
|---|---------|-------------|----------|----------|---------|
| A | 1       | 1           | 0        | 0        |         |
| B | 0       | 1           | 1        | 2        |         |
| C | 3       | 1           | 0        | 0        |         |
| D | 0       | 0           | 1        | 0        |         |
| E | 2       | 1           | 1        | 0        |         |

Resources still needed

E = (6342)  
P = (5322)  
A = (1020)

Example of banker's algorithm with multiple resources

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## Banker's algorithm: data structures

Let  $n$  = number of processes, and  $m$  = number of resources types.

- ◆ **Available:** Vector of length  $m$ . If  $avail[j] = k$ , there are  $k$  instances of resource type  $R_j$  available.
- ◆ **Max:**  $n \times m$  matrix. If  $max[i,j] = k$ , then process  $P_j$  may request at most  $k$  instances of resource type  $R_i$ .
- ◆ **Allocation:**  $n \times m$  matrix. If  $alloc[i,j] = k$  then  $P_j$  is currently allocated  $k$  instances of  $R_i$ .
- ◆ **Need:**  $n \times m$  matrix. If  $Need[i,j] = k$ , then  $P_j$  may need  $k$  more instances of  $R_i$  to complete its task.

$$Need[i,j] = Max[i,j] - Allocation[i,j].$$

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## Banker's algorithm

```
class ResourceMgr {
private:
 Lock lock;
 CV cv;
 int r; // Number of resources
 int t; // Number of threads
 int avail[]; // avail[i]: instances of resource i available
 int max[][]; // max[i][j]: max of resource i needed by thread j
 int alloc[][]; // alloc[i][j]: current allocation of resource i to thread j
 ...
}

// Invariant: the system is in a safe state.
ResourceMgr::Request(int resourceID, int threadID) {
 lock.Acquire();
 assert(isSafe());
 while (!wouldBeSafe(resourceID, threadID)) {
 cv.Wait(&lock);
 }
 alloc[resourceID][threadID]++;
 avail[resourceID]--;
 assert(isSafe());
 lock.Release();
}
```

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## Banker's algorithm (cont'd)

```
// A state is safe iff there exists a safe sequence of grants that are sufficient
// to allow all threads to eventually receive their maximum resource needs.
bool ResourceMgr::isSafe() {
 int j;
 int toBeAvail[] = copy avail[];
 int need[][] = max[][] - alloc[]; // need[i][j] is initialized to max[i][j] - alloc[i][j]
 bool finish[] = {false, false, false, ...}; // finish[j] is true if thread j is guaranteed to finish
 while (true) {
 j = any threadID such that:
 (finish[j] == false) && forall i: need[i][j] <= toBeAvail[i];
 if (no such j exists) {
 if (forall j: finish[j] == true) {
 return true;
 } else {
 return false;
 }
 } else { // Thread j will eventually finish and return its current allocation to the pool.
 finish[j] = true;
 forall i: toBeAvail[i] = toBeAvail[i] + alloc[i][j];
 }
 }
}
```

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## Banker's algorithm (cont'd)

```
// Hypothetically grant request and see if resulting state is safe.
bool
ResourceMgr::wouldBeSafe(int resourceID, int threadID) {
 bool result = false;

 avail[resourceID]--;
 alloc[resourceID][threadID]++;
 if (isSafe()) {
 result = true;
 }
 avail[resourceID]++;
 alloc[resourceID][threadID]--;
 return result;
}
```

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## Why we need Banker's algorithm?

8 pages of memory available

Three processes: A, B, C which need 4, 5, 5 pages respectively

The following would leads to deadlock

| Process | Allocation |   |   |   |   |   |   |   |   |      |      |      |
|---------|------------|---|---|---|---|---|---|---|---|------|------|------|
| A       | 0          | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 3    | wait | wait |
| B       | 0          | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3    | 3    | wait |
| C       | 0          | 0 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | wait | wait | wait |
| Total   | 0          | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 8    | 8    | 8    |

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## Why we need Banker's algorithm?

8 pages of memory available

Three processes: A, B, C which need 4, 5, 5 pages respectively

The following would work!

| Process | Allocation |   |   |   |   |   |   |   |      |      |      |      |
|---------|------------|---|---|---|---|---|---|---|------|------|------|------|
| A       | 0          | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3    | 3    | 4    | 0    |
| B       | 0          | 0 | 1 | 1 | 1 | 2 | 2 | 2 | wait | wait | wait | wait |
| C       | 0          | 0 | 0 | 1 | 1 | 1 | 2 | 2 | 2    | wait | wait | wait |
| Total   | 0          | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 7    | 7    | 8    | 4    |

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## Detect and repair

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- ◆ Algorithm
  - Scan wait for graph
  - Detect cycles
  - Fix cycles
- ◆ Proceed without the resource
  - Requires robust exception handling code
- ◆ Roll back and retry
  - Transaction: all operations are provisional until have all required resources to complete operation